

Homework

- Project: [CoNLL 2004 shared task](#)
- Homework for next week:
 - ★ Download code and data
 - ★ Modify Erik's baseline script to handle double object constructions (or write your own)
 - ★ Read Manning and Schütze, pp. 597–604

1

Committee machines

- Committee machines (or ensemble machines) combine the predictions of more than one classifier
- Committee machines depend on the members being reasonably accurate (better than guessing) and diverse (errors are uncorrelated)
- Majority vote and weighted majority are simple ensemble methods
- Committee machines reduce statistical error, computational error, and representational error

2

Bagging

- Given training data and a learning method, how do we generate a diverse committee of classifiers?
- We can inject randomness into the learning procedure by varying initial conditions or hyperparameters
- *Bagging* (bootstrap aggregation): randomly generate lots (25–200) of training sets by sampling the original training data with replacement majority vote
- Reduces variance, so most effective for high variance, low bias classifiers

3

Error-correcting output coding

- Error-correcting output codes are redundant encodings which allow reliable data transmission in the presence of noise
- They let us generate diverse classifiers by manipulating the target function
- Exhaustive codes work for a small number of class (3–10), otherwise random codes perform well on average
- ECOC classification reduces bias and variance
- Can be combined with other methods (e.g., bagging) to reduce error rate even further

4

Boosting

- Boosting iteratively increases the performance of a weak base learner
- AdaBoost (Adaptive Boosting) constructs a series of classifiers by re-weighting the training data
- Weight for misclassified items are increased and for correctly classified items are decreased
- The training distribution is shifted to emphasize the 'hard' cases
- Final result is a majority vote, weighted by accuracy

5

AdaBoost

- Initialize weights w_i to $1/N$, $i = 1, \dots, N$
- For $m = 1$ to M
 - ★ fit a classifier $G_m(X)$ to X using weights $w_i^{(m)}$
 - ★ compute training error: $\epsilon_m = \sum w_i^{(m)} I(y_i \neq G_m(x_i))$
 - ★ compute $\alpha_m = \frac{1}{2} \log \frac{1-\epsilon_m}{\epsilon_m}$
 - ★ set new weights:

$$w_i^{(m+1)} = \frac{w_i^{(m)} \exp[-\alpha_m y_i G_m(x_i)]}{Z_m}, \quad i = 1, \dots, N$$

- Return

$$G(x) = \text{sign} \left[\sum_m \alpha_m G_m(x) \right]$$

6

AdaBoost

- The training error of G is bounded by:

$$\begin{aligned} \frac{1}{N} \sum I(y_i \neq G(x_i)) &\leq \frac{1}{N} \sum \exp[-y_i \sum_m \alpha_m G_m(x_i)] \\ &\leq \exp[-2 \sum_m \gamma_m^2] \end{aligned}$$

where

$$\gamma_m = \frac{1}{2} - \epsilon_m$$

- As long as $\gamma_m \leq \frac{1}{2}$, the overall error rate will drop exponentially

7

AdaBoost

- Weak learners can be very simple (decision stumps)
- AdaBoost performs extremely well, sometimes considered the best black-box learning method
- Why it works so well has been a bit of a mystery, spurring some important theoretical advances
- Extensions to multiclass classifiers and regression
- Demo [applet](#)

8

AdaBoost

- AdaBoost continues to decrease generalization error even after training error is zero
- The *margin* is a measure of the confidence in a classification:

$$\text{margin}_G(x, y) = \frac{y \sum \alpha_m G_m(x)}{\sum |\alpha_m|}$$

- Shapire, et al. (1998) show that for any $\theta > 0$ the generalization error is at most:

$$R[G] \leq P[\text{margin}_G(x, y) \leq \theta] + \tilde{O}\left(\sqrt{\frac{d}{N\theta^2}}\right)$$

- This bound doesn't depend on M , so extra iterations need not increase the generalization error

9

Exponential loss

- What is AdaBoost really doing?
- Consider an alternative algorithm: forward stagewise additive modeling

- ★ Initialize $f_0(x) = 0$
- ★ For $m = 1$ to M
 - * Compute

$$(\alpha_m, \gamma_m) = \underset{\alpha, \gamma}{\operatorname{argmin}} \sum_i L(y_i, f_{m-1}(x_i) + \alpha b(x_i; \gamma_i))$$

- * Set $f_m = f_{m-1}(x) + \alpha_m b(x; \gamma_m)$

- This will construct a function f which is a sum of basis functions $b(x; \gamma)$ and minimizes the loss function L

10

Exponential loss

- Suppose the basis functions are our weak classifiers G_i , and the loss function is:

$$L(y, f(x)) = \exp(-y f(x))$$

- Then, the update becomes:

$$\begin{aligned} (\alpha_m, G_m) &= \underset{\alpha, G}{\operatorname{argmin}} \sum_i \exp[-y_i (f_{m-1}(x_i) + \alpha G(x_i))] \\ &= \underset{\alpha, G}{\operatorname{argmin}} \sum_i w_i \exp(-\alpha y_i G(x_i)) \end{aligned}$$

where

$$w_i = \exp(-y_i f_{m-1}(x_i))$$

11

Exponential loss

- To solve this, note that:

$$\begin{aligned} \sum_i w_i \exp(-\alpha y_i G(x_i)) &= e^{-\alpha} \sum_{y_i=G(x_i)} w_i + e^{\alpha} \sum_{y_i \neq G(x_i)} w_i \\ &= (e^{\alpha} - e^{-\alpha}) \sum_i w_i I(y_i \neq G(x_i)) + e^{-\alpha} \sum_i w_i \end{aligned}$$

- So, minimizing with respect to G_m gives us:

$$G_m = \underset{G}{\operatorname{argmin}} \sum_i w_i I(y_i \neq G(x_i))$$

- Now if we solve for α , we get (where ϵ_m is the weighted training error rate of G_m):

$$\alpha_m = \frac{1}{2} \log \frac{1 - \epsilon_m}{\epsilon_m}$$

12

Exponential loss

- Now we update the f :

$$f_m(x) = f_{m-1}(x) + \alpha_m G_m(x)$$

- This means the weights on the next round will be:

$$w_i^{(m+1)} = w_i^{(m)} \exp[-\alpha_m y_i G_m(x_i)]$$

- ... which is AdaBoost!
- So, AdaBoost is a greedy algorithm to construct an additive combination of G 's which minimizes the exponential loss:

$$L(y, f(x)) = \exp(-y f(x))$$

13

Exponential loss

- This equivalence shows how boosting relates to other machine learning methods
- It also points to ways AdaBoost could be improved
- Minimizing the exponential loss is the same as maximizing the (population) log likelihood:

$$L(Y, f(x)) = -\log(1 + \exp(-2Y f(x)))$$

- A new algorithm *LogitBoost* maximizes this log likelihood using Newton-style updates (Friedman, Hastie, and Tibshirani 2000)

15

Exponential loss

- Why exponential loss? Mainly, because it's an upper bound on training error which is easy to work with
- Also, it can be shown that:

$$\operatorname{argmin}_{f(x)} E_{Y|x}[\exp(-Y f(x))] = \frac{1}{2} \log \frac{P(Y = 1|x)}{P(Y = -1|x)}$$

- By minimizing the exponential loss, we're estimating (one half of) the log odds of $P(Y = 1|x)$
- Also, note that:

$$P(Y = 1|x) = \frac{\exp f(x)}{\exp -f(x) + \exp f(x)} = \frac{1}{1 + \exp -2f(x)}$$

14

Interpreting models

- One strength of tree-based classifiers is their simple structure, which makes them easy to interpret
- In data mining applications, we are often more interested in the structure that a classifier discovers in the training data than in the accuracy of the rule itself
- Committee machines are virtually impossible to interpret, even if the base learners are simple
- We can measure the relative importance of a variable by summing the estimated error reduction at each node, averaged over all trees in an ensemble

16

Boosting

- Boosting is a very powerful method, which reduces bias and variance, produces very lower error rates, and is highly resistant to overtraining
- Boosting finds an additive collection of basis functions which minimizes the exponential loss (and therefore training error)
- Boosting increase the *margin*, so generalization improves even after the training error reaches zero
- Boosting is more closely related to logistic regression and maximum entropy models than to other committee methods
- There are other things that boosting turns out to be the same as (game theoretic interpretations, etc.)

17

Committee machines

- Bagging and boosting are the best known committee machine methods, but there are others
- *Twicing* (Tukey 1977) fits a model to the data, then fits a model to the errors
- *Stacking* (Wolpert 1992) uses leave-one-out cross validation to construct and weight models (*jackknife*)
- *Bumping* (Tibshirani and Knight 1999) is like bagging, but uses the best single model rather than averaging all of them
- *Arcing* (Breiman 1998) is a hybrid of bagging and boosting
- *Random forests* (Breiman 1999) are a collection of trees built using randomly selected subsets of features

18

Self-training

- A variant of the committee machine model can be used to take advantage of unannotated or semi-annotated data
- Simple self-training uses the output of a classifier as the input to the next round of training (helps a little, but not much)
- If we have more than one classifier, we can improve this:
 - ★ Construct classifiers using training data
 - ★ Classify unannotated examples
 - ★ If enough learners agree on the classification of an example, add it to the training set
 - ★ Repeat.

19

Co-training

- Co-training (Blum and Mitchell 1998) splits features into independent subsets:
 - ★ Train two classifiers using these independent feature sets, to get two independent classifiers A and B
 - ★ Use A to classify unlabeled data, and collect positive and negative examples with the highest classification confidence
 - ★ Do the same with B , and add the newly labeled data to the training sample
 - ★ Repeat
- Use a combination of A and B as final classifier

20

Co-training

- When the independent feature sets satisfy some basic assumptions, co-training can improve a weak initial hypothesis to arbitrary accuracy
- Even when feature sets aren't independent (e.g., randomly selected words in a bag-of-words model), co-training works well
- All these methods can be improved significantly by *active learning*
- These semi-supervised learning methods allow more efficient use of (expensive, slow) human annotators

21

Generalization

- What happened to the curse of dimensionality?
- Dimensionality (as number of features) has no clear interpretation for complex modeling procedures
- And what about simplicity? Didn't we say simpler = lower variance?
- How is an ensemble of trees simpler than a single tree?
- How is MaxEnt simpler than Naive Bayes?
- How is MaxEnt+prior simpler than MaxEnt?

23

Committee machines

- Combinations of classifiers can perform better than any one classifier, so long as:
 - ★ each classifier is more accurate than randomly guessing
 - ★ the errors made by each classifier are uncorrelated
- Various strategies for producing useful committees
- Committee machines reduce variance, and sometimes reduce bias as well
- Some committee methods are related to other classifiers in interesting ways
- Committee methods can also be used to take advantage of unannotated or partially annotated data

22

Generalization

- Notions like dimensionality and simplicity aren't really what we're interested in
- Dimensionality reduction and simplification are meant to improve *generalization* – the ability to abstract away from accidental details of a training sample
- A better way to get at that is by restricting *capacity*
- Deleting features or simplifying models may (or may not) reduce the representational capacity of a model

24

Generalization

- Take MaxEnt models with a Gaussian prior:

$$\lambda^* = \operatorname{argmax}_{\lambda} L(\lambda) - \frac{1}{2\sigma^2} \sum_i \lambda_i^2$$

- This is equivalent to:

$$\lambda^* = \operatorname{argmax}_{\lambda} L(\lambda)$$

where

$$\sum_i \lambda_i^2 \leq s^2$$

- The solution is the point which maximizes L and falls inside the hypersphere with radius s
- The prior reduces the capacity of the model, which (empirically) improves generalization